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## Runout of submarine landslide simulated with material point method

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### Abstract

Most of the present knowledge on submarine landslides relies upon back-analysis of post-failure deposits identified using geophysical techniques. In this paper, the runout of slides on rigid bases is explored using the material point method with focus on the geotechnical aspects of the morphologies. In MPM, the sliding material and bases are discretised into a number of Lagrangian particles, and a background Eulerian mesh is employed to update the state of the particles. The morphologies of the slide can be reproduced by tracking the Lagrangian particles in the dynamic processes. A real case history of a submarine slide is back-analyzed with the MPM and also a depth-averaged method. Runout of the slides from steep slopes to moderate bases are reproduced. Then different combinations of soil and basal parameters are assumed to trigger runout mechanisms of elongation, block sliding and spreading. The runout distances predicted by the MPM match well with those from large deformation finite element analysis for the elongation and block sliding patterns. Horst and grabens are shaped in a spreading pattern. However, the current MPM simulations for materials with high sensitivities are relatively mesh sensitive.

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### 1. Introduction

Submarine landslides are one of the most hazardous geological threats to subsea infrastructure, since they can transport vast volumes of sediments across continental slopes. Velocities of the slides can be up to 20 m/s, reaching final runout distances of hundreds of kilometers [1]. Most of the present knowledge on submarine slide relies upon

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back-analysis of post-failure deposits identified using geophysical techniques. Although various conceptual models have been proposed to analyze the runout mechanisms of slides, work on the runout process and evolution of morphologies remains limited. A variety of failure patterns have been reported: retrogressive failure in the Storegga slide generated a series of grabens and ridges [2]; failure starting from the toe and progressing towards the head scarps was found together with compressional and extensional distortion [3]; and out-runner blocks were observed in the Tampen slide [4]. In this paper, the runout of submarine slides is simulated using the material point method (MPM). A real case history of a submarine slide is back-analysed with the MPM and also with a depth-averaged method (DAM). The runout morphologies predicted by the two methods are compared. Then different combinations of soil and seabed parameters are explored to trigger runout mechanisms of elongation, block sliding and spreading. The runout distances predicted by the MPM are compared with those from large deformation finite element (LDFE) analysis.

## 2. Methodology

The MPM, originating from the particle-in-cell method in computational fluid dynamics [5], can be regarded as a combination of finite element and meshfree methods. It possesses an inherent advantage for large deformation problems such as runout of landslides [6] and large-amplitude displacements of structural elements in soil [7], by means of discretising soil as Lagrangian particles. The material mechanical and kinematic properties (mass, volume, density, velocities, momentum, deformation gradients and stresses) are recorded and updated at the particles, and an Eulerian mesh is used for calculation in each incremental step only. Since the mesh is fixed in space, mesh entanglement such as occurs in conventional finite element methods is avoided. An in-house MPM program was developed, which stems from an open-source package Uintah [8] but was enhanced with a novel contact algorithm ‘Geo-contact’ [9] and a GPU parallel computing strategy [10]. The updated Lagrangian calculation in explicit integration is based on the generalised interpolation material point method presented in [11].

The interaction between the slide and rigid base was considered with the ‘Geo-contact’ by adjusting the nodal velocities of the slide. The slide and base might be in contact at specific nodes if both of their masses projected onto the nodes are non-zero. For a specific slide node in contact, the normal velocity  $v^n$  was eliminated; and the tangential velocity  $v^t$  was reduced by

$$\Delta v^t = \min\left(v^t, \frac{\tau A \Delta t}{m}\right) \quad (1)$$

where  $\tau$  is the maximum shear stress on the interface;  $A$  and  $m$  are respectively the area and mass represented by the node;  $\Delta t$  is the time increment, determined through the Courant-Friedrichs-Lewy stability condition. In the following simulations, the tangential behaviour of the slide-base interface is regarded as: (i) No-slip: the slide is fixed at the interface with  $\tau$  limited only by the strength of adjacent material. (ii) Frictional: a maximum shear stress  $\tau$ , potentially lower than the strength of adjacent material, is specified along the interface.

Strain-softening and rate-dependency of the undrained shear strength of slides are expressed in multiplicative (Eq. 2) or additive (Eq. 3) form according to

$$s_u = s_{u0} \left\{ \left[ \delta_{rem} + (1 - \delta_{rem}) e^{-3\xi / \xi_{95}} \right] + \eta \left( \frac{\dot{\gamma}}{\dot{\gamma}_{ref}} \right)^n \right\} \quad (2)$$

$$s_u = s_{u0} \left[ \delta_{rem} + (1 - \delta_{rem}) e^{-3\xi / \xi_{95}} \right] \left\{ 1 + \eta \left( \frac{\dot{\gamma}}{\dot{\gamma}_{ref}} \right)^n \right\} \quad (3)$$

where  $s_{u0}$  is the threshold shear strength,  $\delta_{rem}$  the strength ratio between the fully-remoulded and intact state (i.e. inverse of sensitivity  $S_t$ ),  $\zeta$  the cumulative plastic shear strain with  $\zeta_{95}$  the plastic shear strain required to achieve 95% of remoulding,  $\eta$  the viscosity coefficient and  $n$  the shear-thinning index,  $\dot{\gamma}$  the shear strain rate and  $\dot{\gamma}_{ref}$  the reference shear strain rate. In all simulations with the MPM, a  $4 \times 4$  particle configuration was allocated for each element fully occupied by particles prior to the calculation. The particle density was finer than the  $2 \times 2$  particle configuration used in [9] and [10], to improve the numerical accuracy. The acceleration of gravity was  $g = 9.81 \text{ m/s}^2$ . The Poisson's ratio of the soils was taken as 0.49 to approximate constant volume under assumed undrained conditions. The Young's modulus was taken as  $100s_{u0}$ . The time step  $\Delta t$  was determined by a Courant number of 0.3.

The DAM uses layer-integrated governing equations to describe the conservation of mass and momentum [12], simplifying two-dimensional runout into a one-dimensional (1D) problem. This simplification is acceptable for large scale events, where shallow water approximations to the Navier-Stokes equations are acceptable for overall behaviour of the runout. This approach is especially attractive on computational efficiency, requiring orders of magnitude less effort than other approaches. The volume of mass is discretized into a number of Lagrangian elements, which are solved, for example, using an explicit time-marching finite difference scheme. Each element advances at the local layer-averaged velocity. The thickness of each element is computed at the mid-point, but the volume remains constant.

The large deformation finite element (LDFE) approach used in the following study is the one termed 'remeshing and interpolation technique by small strain (RITSS)' developed at the University of Western Australia [13, 14]. The basic procedure is to divide the runout of the slides into hundreds or thousands incremental steps. The time step must be sufficiently small that all slide elements maintain acceptable shape during each step, then an updated Lagrangian calculation in the implicit integration scheme is performed. After that, the deformed slides are remeshed and the stresses and material properties at integration points and the nodal velocities and accelerations are mapped from the old mesh to the new mesh. The commercial FE package, Abaqus, was used to conduct mesh generation and Lagrangian calculations.

### 3. Back-analysis of a real case

A real case history of submarine escarpment failure in the southern Mediterranean<sup>1</sup> was back-analysed with the MPM and DAM with the idealized geometries shown in Fig. 1(a). The failure was triggered by a steep slope at an inclination of  $13.75^\circ$  to the horizontal and the runout on a gently-inclined base reached a final distance of  $\sim 420 \text{ m}$ . The slide-base interface was assumed as no-slip. The submerged density of the slide was  $525 \text{ kg/m}^3$ . The shear strength of the slide was approximated with Eq. 2, with  $s_{u0} = 15 \text{ kPa}$ ,  $\delta_{rem} = 0.025$  ( $S_t = 40$ ),  $\zeta_{95} = 45$ , viscosity coefficient  $\eta = 0.0167$ , shear-thinning index  $n = 0.5$  and reference strain rate  $\dot{\gamma}_{ref} = 1 \text{ s}^{-1}$ .

In the MPM analysis, the element size was  $0.2 \text{ m}$ , i.e.  $\sim H_0/60$ , which is sufficiently fine by trial calculations.  $H_0$  represents the initial height of the slide. In total, there were 560,700 and 16,400 particles for the slide and base, respectively. The runout distances predicted by the DAM and MPM are close to the field observation (see Fig. 1(b)). But less mobility of the runout is predicted by the DAM than by the MPM: the peak velocities predicted by the DAM are approximately half those of the MPM predictions; the runout of the softening soil in the DAM analysis is delayed till 54 s, much later than the instant mobilisation in the MPM analysis. This is mainly attributed to the over-simplification of estimating the shear strain rate of the 1D element in the DAM analysis, which is derived from the ratio of the velocity difference between the top and bottom nodes to the thickness of the element. This simplification implies that the velocity profiles are linear within the shear layer; this over-estimates the thickness of the shear layer.

The runout morphologies predicted by the DAM and MPM analyses are similar, as shown in Fig. 2. The failure is triggered at the front toe of the sliding mass and then retrogressively extends to the head. The runout from the steep slope is initially stacked in front of the steep slope and then elongates along the gently-inclined base. Part of the

<sup>1</sup> The information of the real case was provided by Dr Spinewine Benoit from Fugro GeoConsulting. The DAM simulations were performed by Dr Spinewine Benoit together with Dr Sam Ingarfield from Fugro AG Pty Ltd.

original slide hangs on the slope as a relict due to the no-slip basal interface. The thickness of the slide decreases with elongation in length, which causes a larger resistance along the basal interface. Due to the strain-softening, the slide shrinks at toe of the steep slope.

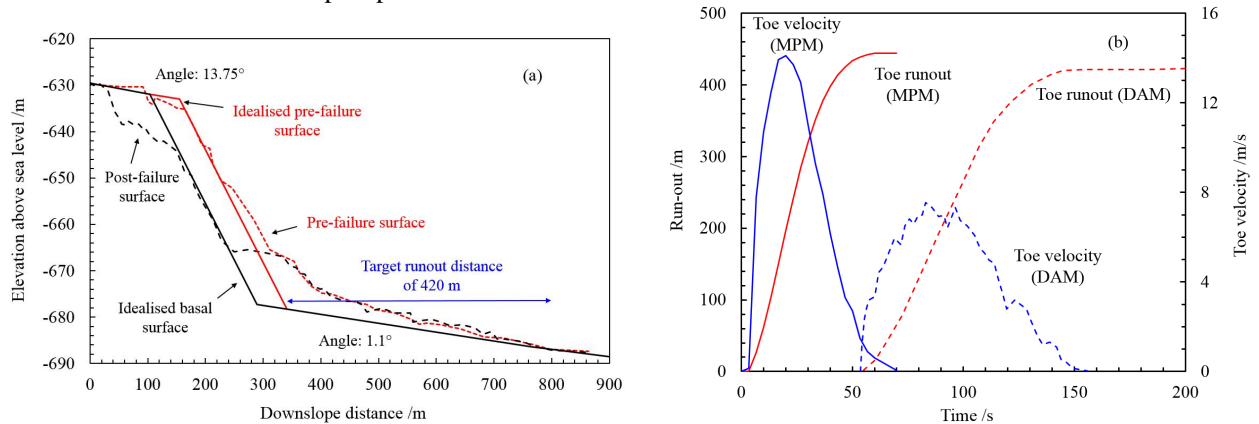


Fig. 1. (a) Idealization of slide transect; (b) History of toe velocity and runout.

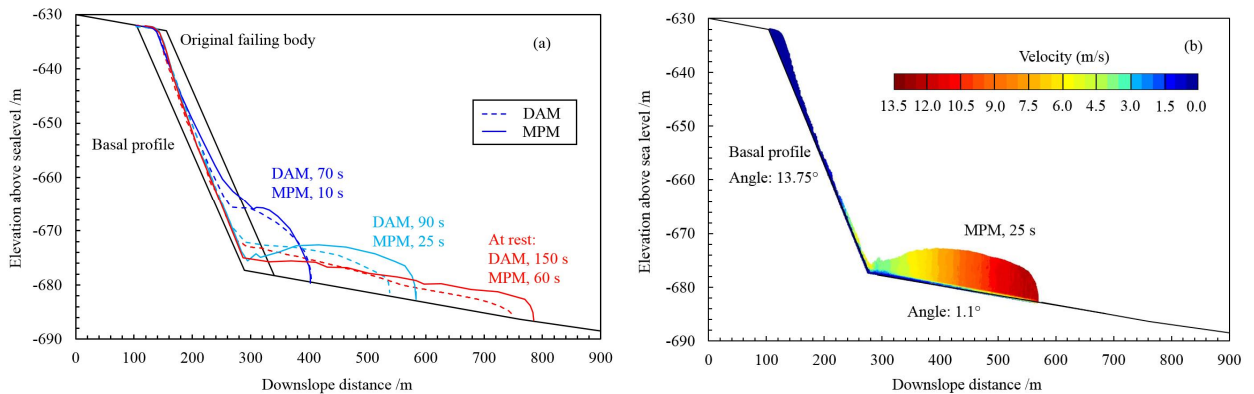


Fig. 2. (a) Evolution of runout morphologies; (b) Velocity contours by MPM at 25 s.

#### 4. Parametric studies

Four cases were designed to further study the runout morphologies<sup>2</sup> of planar submarine slides, based on an idealised geometry of original slides defined in Figure 3. The slide material was initially trapezoidal in shape with side-slopes of 30°, placed on a slope with an angle  $\theta$  to the horizontal. The height and length of the sliding mass were 5 m and 48.66 m, respectively. The runout behaviour depends on the combined influence of geometry and material properties of the slide, slope inclination and slide-base interaction. The parameters varied are listed in Table 1. For all analyses the submerged density of the sliding mass was  $\rho' = 600 \text{ kg/m}^3$ . The shear strength of the slide was approximated by Eq. 3. In the MPM analyses, the size of the square elements was selected as 0.1 m unless otherwise stated. In total, there were 307,200 slide particles and 6,000 base particles. Three flow mechanisms, elongation, block sliding and spreading, were observed through the cases in Table 1. Mesh dependency is detected in the spreading pattern due to strain-localisation for softening soil, while it is not observed in elongation and block sliding patterns for non-softening soils.

<sup>2</sup> The LDFE simulation of runout mechanisms of elongation, block sliding and spreading were originally discussed in [15]

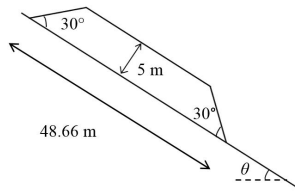


Fig. 3. Problem definition for parametric study of runout behaviour (not to scale).

Table 1. Configurations of submarine slide cases.

Case	$\theta$ (°)	$s_{u0}$ (kPa)	$\eta$	$n$	$\dot{\gamma}_{ref}$	$S_t$	$\zeta_{95}$	Slide-base interface	Runout mechanism
1	5	2.5	-	-	-	1	-	$\tau = 1$ kPa	Elongation
2	5	2.5	-	-	-	1	-	No-slip	Elongation
3	5	2.5	1	0.1	0.01	1	-	$\tau = 1$ kPa	Block sliding
4	2	5	-	-	-	40	5	$\tau = 1$ kPa	Spreading

#### 4.1. Elongation

The soils in Cases 1 and 2 have a constant shear strength of 2.5 kPa, i.e. rate-dependency and strain-softening are ignored. The only difference between the two cases is the slide-base interface, which is frictional with a shear strength of 1 kPa for Case 1 and no-slip for Case 2. The sliding masses in Case 1 and 2 move forward along the base, driven by the relative magnitudes of the self-weight and the friction on the interface. The rear parts of the masses collapse since unsupported. The sliding masses elongate and the thicknesses reduce, as shown in Fig. 4(a) for Case 1. The frictional resistance along the slide-base interface thus increases due to the lengthened interface. The runout decelerates once the total friction on the interface exceeds the driving force due to the self-weight. The simulation of Case 1 was terminated before the runout had stopped, due to the heavy computational effort. The runout in Case 2 stops at time  $\sim 13$  s. As shown in Fig. 4(b), similar final runout distances of  $\sim 22$  m in Case 2 were predicted by the LDFE and the MPM analyses. Velocity contours predicted by the MPM for Case 1 at 15 s is shown in Fig. 5.

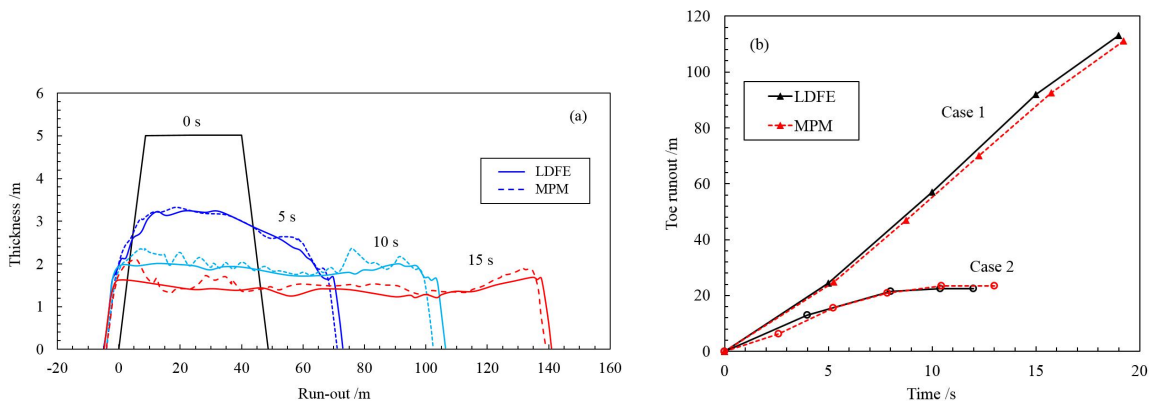


Fig. 4. (a) Evolution of runout morphologies; (b) History of toe velocity and runout.

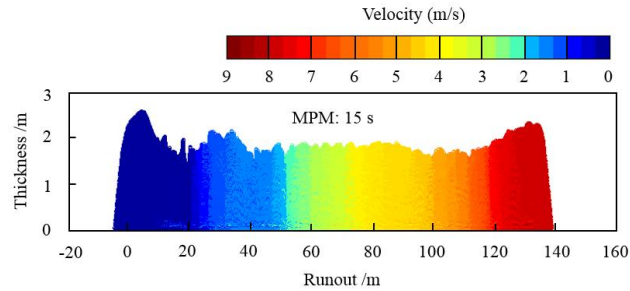


Fig. 5. Velocity contours predicted by MPM for Case 1 at 15 s.

#### 4.2. Block sliding

The soil in Case 3 was assumed as rate-dependent but strain-softening was not considered. In general the shear strength of the slide was increased by a factor of up to  $\sim 2.5$  compared with the threshold shear strength. The height of the sliding mass reduces only slowly, so that the slide moves essentially as a block. The driving shear stress on the basal interface reduces from  $> 4.1$  kPa to  $\sim 2.1$  kPa, which is still larger than the maximum shear stress  $\tau$  on the interface. The slide continues to accelerate, achieving a toe velocity of 9.7 m/s at 40 s and a toe runout of  $\sim 300$  m (but with the slide still moving when the computation was terminated). The runout morphologies and distances predicted by the LDFE and MPM analyses are similar, as shown in Fig. 6(a). Velocity contours predicted by the MPM analysis are shown in Fig. 6(b).

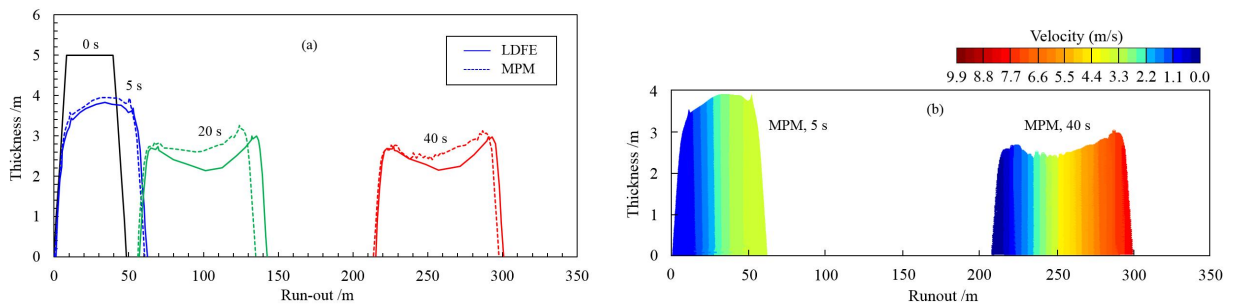


Fig. 6. (a) evolution of runout morphologies; (b) velocity contour predicted by MPM.

#### 4.3. Spreading with horsts and grabens

The soil in Case 4 was assumed as rate-independent, with intact shear strength of 5 kPa and a high sensitivity of 40 (essentially simulating softening by water entrainment as well as remolding). By contrast with the previous cases, the slope inclination was reduced to  $2^\circ$  in Case 4. Fig. 7 shows the initialization and propagation of shear bands in the sliding mass. Soil collapses are initially triggered on both sides of the mass (at 2 s), followed by more failures spread progressively to the middle due to loss of lateral pressure (at 10 s). A series of horsts and grabens are formed with dislocation of the failed soil. The original horsts are inverted V-shaped wedges with two edges at an inclination of  $45^\circ$  to the base. The heavily disturbed soil is localized in the shear bands, while soil in the wedges is only slightly disturbed. The wedges tend to detach from each other due to velocity differences; as a result, the front wedges break away from the main body at 27 s (Fig. 8(a)). The outrunner blocks are expected to reach a very long runout distance as reported in [16]. Therefore, the simulation was terminated at 27 s although the runout distance of 112 m was not finalised.

The propagation of shear bands in the sliding masses is mesh-sensitive due to the weak discontinuity bifurcation properties of constitutive models. Although several regularization mechanisms have been introduced, such as rate-dependent plasticity models, non-local models, gradient models and micro-polar continua models [17], this topic

remains open. Greater mobility is seen for runouts with finer mesh as seen in Fig. 8(b). As a result, the runout distances of the spreading pattern of submarine slides, especially with breakaway of out-runner blocks, cannot be predicted accurately.

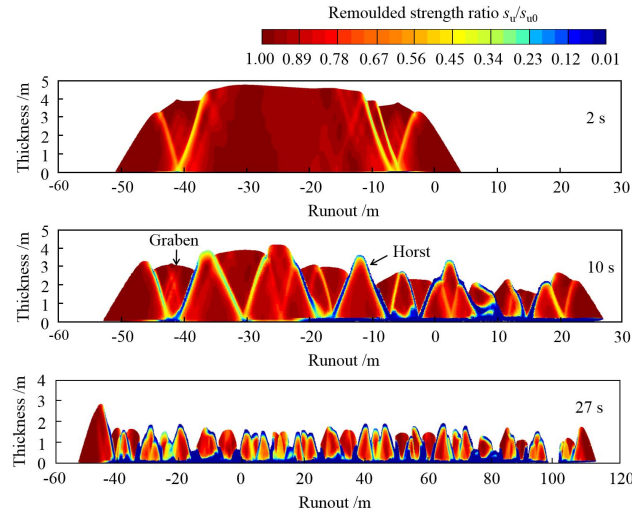


Fig. 7. Evolution of horsts and grabens.

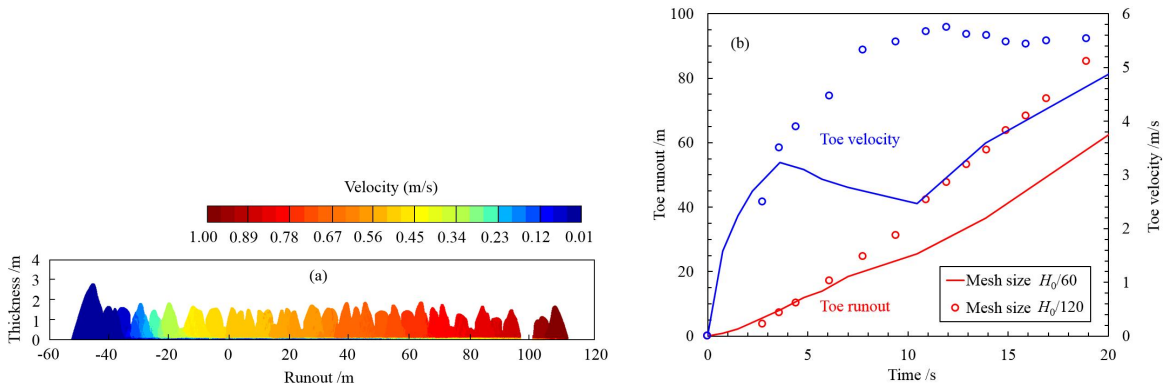


Fig. 8. (a) velocity contour at 27 s; (b) history of toe velocity and runout.

### 5. Conclusions

Numerical simulation of the runout process of submarine slides with the MPM has been performed. A real case history of submarine slide was back-analysed with the MPM and DAM. Greater mobility of the runout was predicted by the MPM compared with the prediction by the DAM. The calculation of shear strain rates in the DAM analysis was considered as over-simplified. Different combinations of soil and seabed parameters were explored to trigger runout mechanisms of elongation, block sliding and spreading. The runout distances predicted by the MPM match well with those from LDFE analysis for the elongation and block sliding patterns. Horst and grabens are formed in the spreading pattern. However, the current MPM simulations for materials with high sensitivities are mesh sensitive.

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